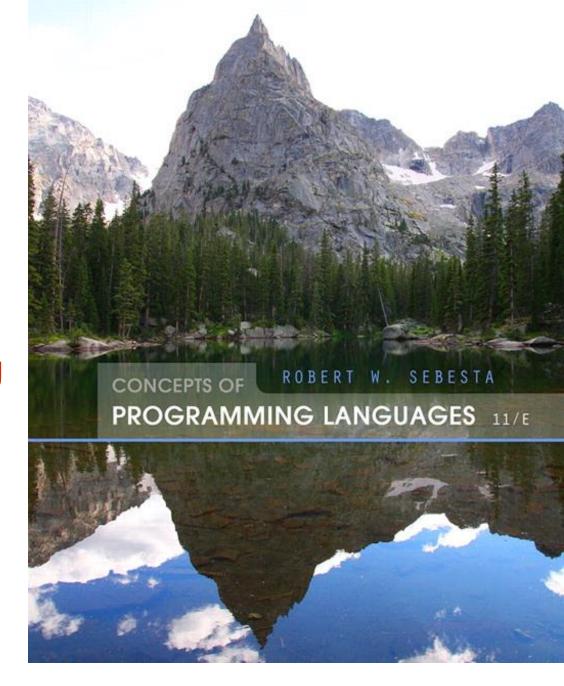
Chapter 16

Logic Programming Languages



Chapter 16 Topics

- Introduction
- A Brief Introduction to Predicate Calculus
- Predicate Calculus and Proving Theorems
- An Overview of Logic Programming
- The Origins of Prolog
- The Basic Elements of Prolog
- Deficiencies of Prolog
- Applications of Logic Programming

Introduction

- Programs in logic languages are expressed in a form of symbolic logic
- Use a logical inferencing process to produce results
- Declarative rather that procedural:
 - Only specification of *results* are stated (not detailed *procedures* for producing them)

Proposition

- A logical statement that may or may not be true
 - Consists of objects and relationships of objects to each other

Symbolic Logic

- Logic which can be used for the basic needs of formal logic:
 - Express propositions
 - Express relationships between propositions
 - Describe how new propositions can be inferred from other propositions
- Particular form of symbolic logic used for logic programming called predicate calculus

Object Representation

- Objects in propositions are represented by simple terms: either constants or variables
- Constant: a symbol that represents an object
- Variable: a symbol that can represent different objects at different times
 - Different from variables in imperative languages

Compound Terms

- Atomic propositions consist of compound terms
- Compound term: one element of a mathematical relation, written like a mathematical function
 - Mathematical function is a mapping
 - Can be written as a table

Parts of a Compound Term

- Compound term composed of two parts
 - Functor: function symbol that names the relationship
 - Ordered list of parameters (tuple)
- Examples:

```
student(jon)
like(seth, OSX)
like(nick, windows)
like(jim, linux)
```

Forms of a Proposition

- Propositions can be stated in two forms:
 - Fact. proposition is assumed to be true
 - Query: truth of proposition is to be determined
- Compound proposition:
 - Have two or more atomic propositions
 - Propositions are connected by operators

Logical Operators

Name	Symbol	Example	Meaning
negation		¬ а	not a
conjunction	\cap	a∩b	a and b
disjunction	U	a∪b	a or b
equivalence		a ≡ b	a is equivalent to b
implication	\supset	$a \supset b$	a implies b
		$a \subset b$	b implies a

Quantifiers

Name	Example	Meaning
universal	∀X.P	For all X, P is true
existential	∃Х.Р	There exists a value of X such that P is true

Clausal Form

- Too many ways to state the same thing
- Use a standard form for propositions
- · Clausal form:
- $B_1 \cup B_2 \cup ... \cup B_n \subset A_1 \cap A_2 \cap ... \cap A_m$
- means if all the As are true, then at least one B is true
- Antecedent. right side
- Consequent. left side

Predicate Calculus and Proving Theorems

- A use of propositions is to discover new theorems that can be inferred from known axioms and theorems
- Resolution: an inference principle that allows inferred propositions to be computed from given propositions

Resolution

- Unification: finding values for variables in propositions that allows matching process to succeed
- Instantiation: assigning temporary values to variables to allow unification to succeed
- After instantiating a variable with a value, if matching fails, may need to backtrack and instantiate with a different value

Proof by Contradiction

- Hypotheses: a set of pertinent propositions
- Goal: negation of theorem stated as a proposition
- Theorem is proved by finding an inconsistency

Theorem Proving

- Basis for logic programming
- When propositions used for resolution, only restricted form can be used
- Horn clause can have only two forms
 - Headed: single atomic proposition on left side
 - Headless: empty left side (used to state facts)
- Most propositions can be stated as Horn clauses

Overview of Logic Programming

- Declarative semantics
 - There is a simple way to determine the meaning of each statement
 - Simpler than the semantics of imperative languages
- Programming is nonprocedural
 - Programs do not state now a result is to be computed, but rather the form of the result

Example: Sorting a List

 Describe the characteristics of a sorted list, not the process of rearranging a list

```
sort(old_list, new_list) ⊂ permute (old_list, new_list) ∩ sorted (new_list)
```

```
sorted (list) \subset \forall_j such that 1 \le j < n, list(j) \le list (j+1)
```

The Origins of Prolog

- University of Aix-Marseille (Calmerauer & Roussel)
 - Natural language processing
- University of Edinburgh (Kowalski)
 - Automated theorem proving

Terms

- This book uses the Edinburgh syntax of Prolog
- Term: a constant, variable, or structure
- Constant: an atom or an integer
- Atom: symbolic value of Prolog
- Atom consists of either:
 - a string of letters, digits, and underscores beginning with a lowercase letter
 - a string of printable ASCII characters delimited by apostrophes

Terms: Variables and Structures

- Variable: any string of letters, digits, and underscores beginning with an uppercase letter
- Instantiation: binding of a variable to a value
 - Lasts only as long as it takes to satisfy one complete goal
- Structure: represents atomic proposition functor (parameter list)

Fact Statements

- Used for the hypotheses
- Headless Horn clauses

```
female(shelley).
male(bill).
father(bill, jake).
```

Rule Statements

- Used for the hypotheses
- Headed Horn clause
- Right side: antecedent (if part)
 - May be single term or conjunction
- Left side: consequent (then part)
 - Must be single term
- Conjunction: multiple terms separated by logical AND operations (implied)

Example Rules

```
ancestor(mary, shelley):- mother(mary, shelley).
```

 Can use variables (universal objects) to generalize meaning:

```
parent(X,Y):- mother(X,Y).

parent(X,Y):- father(X,Y).

grandparent(X,Z):- parent(X,Y), parent(Y,Z).
```

Goal Statements

- For theorem proving, theorem is in form of proposition that we want system to prove or disprove – goal statement
- Same format as headless Horn

```
man(fred)
```

 Conjunctive propositions and propositions with variables also legal goals

```
father (X, mike)
```

Inferencing Process of Prolog

- Queries are called goals
- If a goal is a compound proposition, each of the facts is a subgoal
- To prove a goal is true, must find a chain of inference rules and/or facts. For goal Q:

```
P_2 : - P_1
P_3 : - P_2
...
Q : - P_n
```

 Process of proving a subgoal called matching, satisfying, or resolution

Approaches

- Matching is the process of proving a proposition
- Proving a subgoal is called satisfying the subgoal
- Bottom-up resolution, forward chaining
 - Begin with facts and rules of database and attempt to find sequence that leads to goal
 - Works well with a large set of possibly correct answers
- Top-down resolution, backward chaining
 - Begin with goal and attempt to find sequence that leads to set of facts in database
 - Works well with a small set of possibly correct answers
- Prolog implementations use backward chaining

Subgoal Strategies

- When goal has more than one subgoal, can use either
 - Depth-first search: find a complete proof for the first subgoal before working on others
 - Breadth-first search: work on all subgoals in parallel
- Prolog uses depth-first search
 - Can be done with fewer computer resources

Backtracking

- With a goal with multiple subgoals, if fail to show truth of one of subgoals, reconsider previous subgoal to find an alternative solution: backtracking
- Begin search where previous search left off
- Can take lots of time and space because may find all possible proofs to every subgoal

Simple Arithmetic

- Prolog supports integer variables and integer arithmetic
- is operator: takes an arithmetic expression as right operand and variable as left operand

```
A is B / 17 + C
```

- Not the same as an assignment statement!
 - The following is illegal:

```
Sum is Sum + Number.
```

Example

```
speed (ford, 100).
speed (chevy, 105).
speed (dodge, 95).
speed (volvo, 80).
time (ford, 20).
time (chevy, 21).
time (dodge, 24).
time (volvo, 24).
distance(X,Y) :- speed(X,Speed),
                        time (X, Time),
                        Y is Speed * Time.
```

A query: distance(chevy, Chevy_Distance).

Trace

- Built-in structure that displays instantiations at each step
- Tracing model of execution four events:
 - Call (beginning of attempt to satisfy goal)
 - Exit (when a goal has been satisfied)
 - *Redo* (when backtrack occurs)
 - Fail (when goal fails)

Example

```
likes (jake, chocolate).
likes (jake, apricots).
                                               Call
                                                                     Fail
likes (darcie, licorice).
likes (darcie, apricots).
                                                  likes (jake, X)
trace.
likes (jake, X), likes (darcie, X).
                                               Exit
                                                                     Redo
 (1) 1 Call: likes(jake, 0)?
 (1) 1 Exit: likes(jake, chocolate)
 (2) 1 Call: likes(darcie, chocolate)?
                                               Call
                                                                     Fail
 (2) 1 Fail: likes(darcie, chocolate)
 (1) 1 Redo: likes(jake, 0)?
 (1) 1 Exit: likes(jake, apricots)
                                                 likes (darcie, X)
 (3) 1 Call: likes(darcie, apricots)?
 (3) 1 Exit: likes(darcie, apricots)
X = apricots
                                               Exit
                                                                     Redo
```

List Structures

- Other basic data structure (besides atomic propositions we have already seen): list
- List is a sequence of any number of elements
- Elements can be atoms, atomic propositions, or other terms (including other lists)

Append Example

More Examples

```
reverse([], []).
reverse([Head | Tail], List) :-
    reverse (Tail, Result),
        append (Result, [Head], List).

member(Element, [Element | _]).
member(Element, [_ | List]) :-
        member(Element, List).
```

The underscore character means an anonymous variable—it means we do not care what instantiation it might get from unification

Deficiencies of Prolog

- Resolution order control
 - In a pure logic programming environment, the order of attempted matches is nondeterministic and all matches would be attempted concurrently
 - The closed-world assumption
 - The only knowledge is what is in the database
 - The negation problem
 - Anything not stated in the database is assumed to be false
 - Intrinsic limitations
 - It is easy to state a sort process in logic, but difficult to actually do—it doesn't know how to sort

Applications of Logic Programming

- Relational database management systems
- Expert systems
- Natural language processing

Summary

- Symbolic logic provides basis for logic programming
- Logic programs should be nonprocedural
- Prolog statements are facts, rules, or goals
- Resolution is the primary activity of a Prolog interpreter
- Although there are a number of drawbacks with the current state of logic programming it has been used in a number of areas